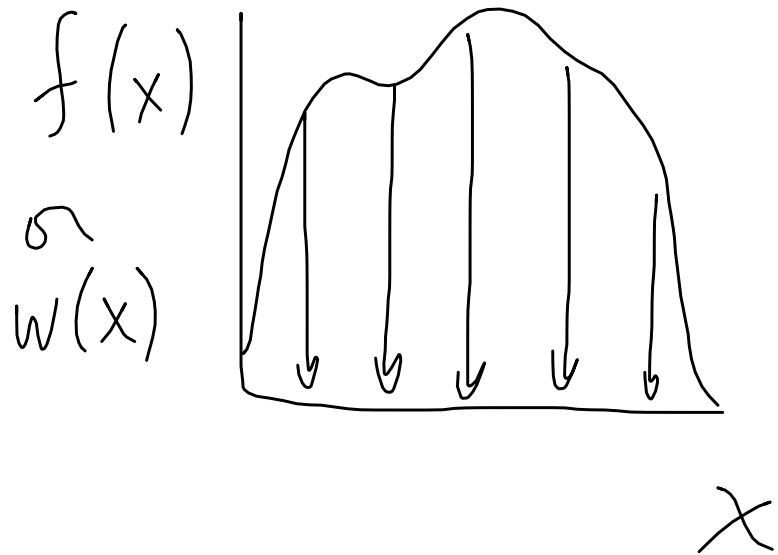


# Distributed forces

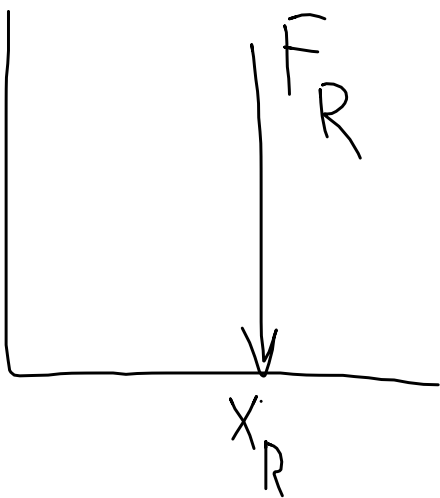


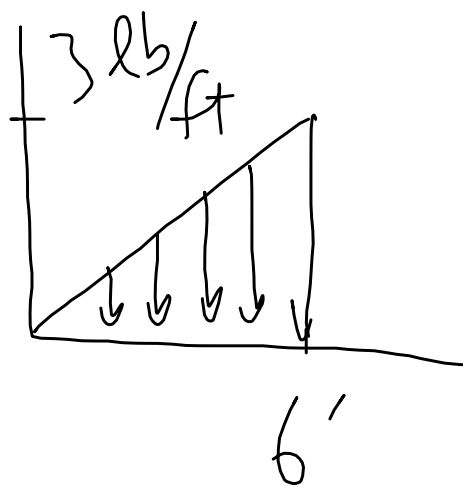
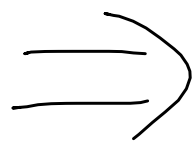
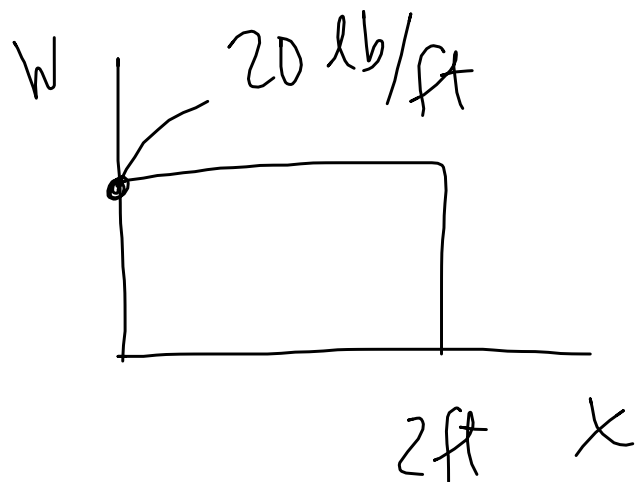
$f \Rightarrow \frac{\text{force}}{\text{length}}$

$$F_R = \int w(x) dx$$

$$M_o = \int x w(x) dx$$

$$x_R = \frac{M_o}{F_R}$$

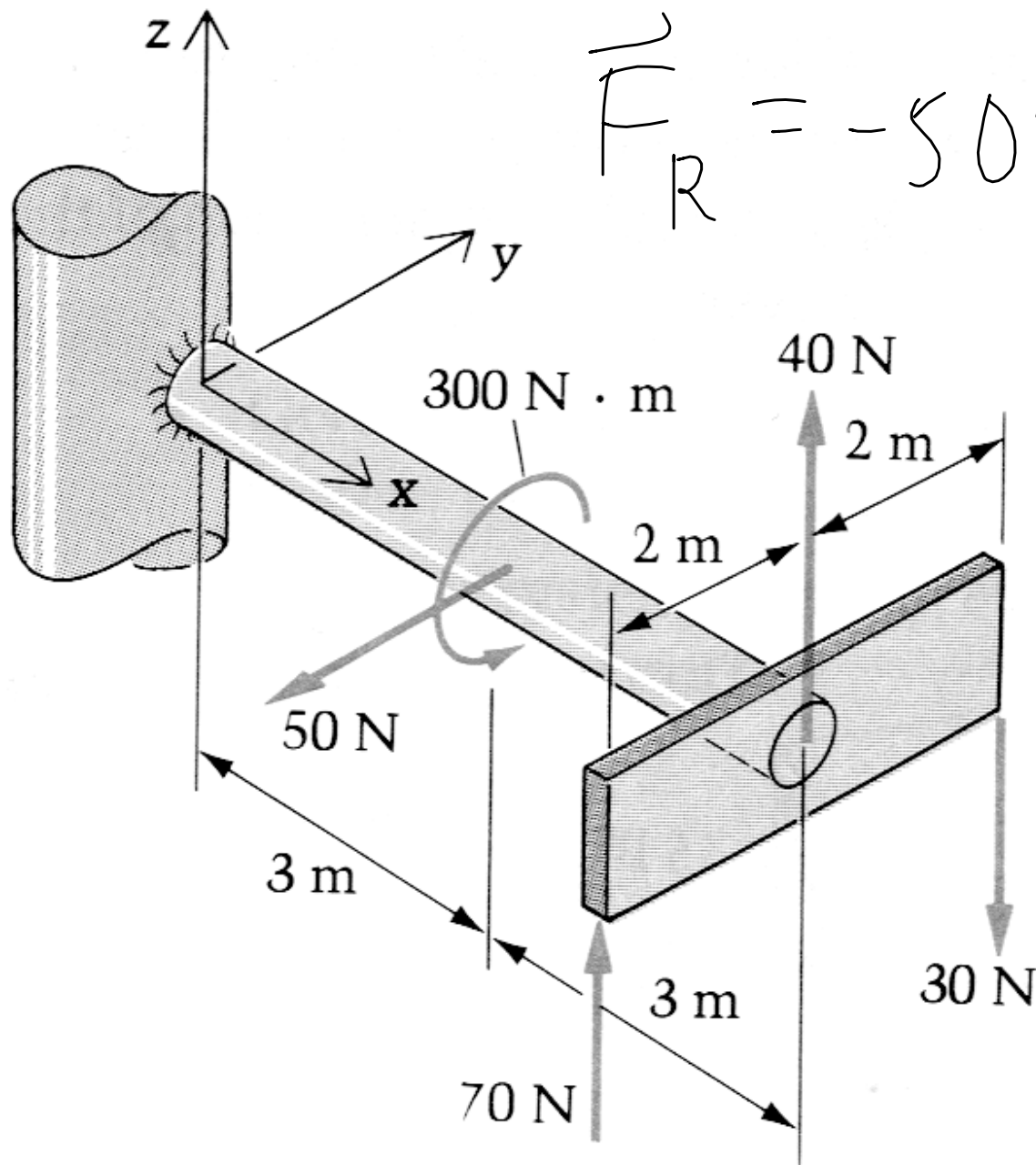




$$F_R = 9 \text{ lbs}$$

$$M_0 = \int_0^6 x w(x) dx = \int_0^6 x \frac{1}{2} x dx = \frac{x^3}{6} \Big|_0^6 = 36 \text{ ft}\cdot\text{lb}$$

$$x_R = \frac{M_0}{F_R} = \frac{36}{9} = 4 \text{ ft} \Rightarrow \frac{2}{3} \text{ from pointy end}$$



$$\vec{F}_R = -50\hat{j} + 80\hat{k}$$

$$\sum \vec{M}_O =$$

$$\hat{i} [300 - 70(2) - 30(2)]$$

$$+ \hat{j} [-70(6) - 40(6) + 30(6)]$$

$$+ \hat{k} [-50(3)]$$

$$= 100\hat{i} - 480\hat{j} - 150\hat{k}$$

Test for single force resultant

$$\vec{M}_O \cdot \vec{F}_R \stackrel{?}{=} 0$$

$$-50(-480) + 80(-150) = 12000 \neq 0 \therefore \text{screwdriver}$$

$$\begin{aligned} \vec{M}_{||} &= (\vec{M}_O \cdot \hat{u}_F) \hat{u}_F \\ &= \left[ (100\hat{i} - 480\hat{j} - 150\hat{k}) \cdot \frac{-50\hat{j} + 80\hat{k}}{\sqrt{8900}} \right] \left( \frac{-50\hat{j} + 80\hat{k}}{\sqrt{8900}} \right) \end{aligned}$$

$$\left[ (-480)(-50) + (-150)(80) \right] \left( \frac{-50\hat{j} + 80\hat{k}}{8900} \right) = \vec{M}_{||}$$

$$-67.42\hat{j} + 107.9\hat{k} = \vec{M}_{||}$$

$$\vec{M}_{\perp} = \vec{M}_0 - \vec{M}_{||}$$

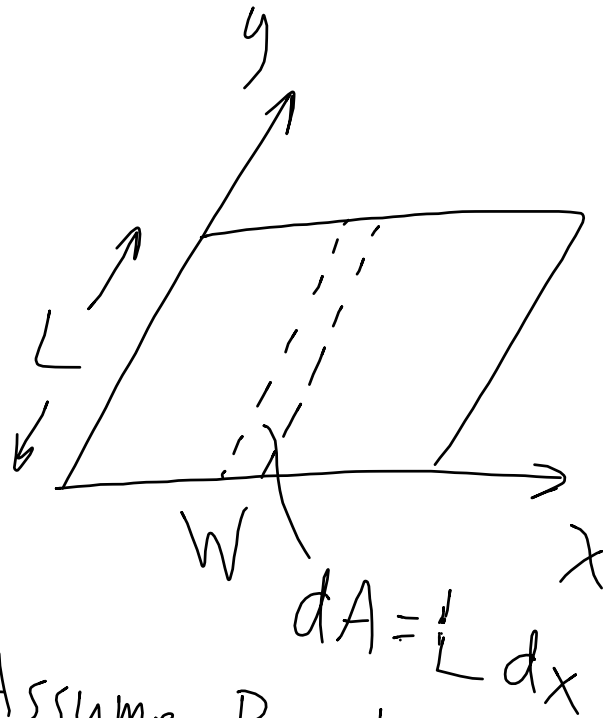
$$= 100\hat{i} - 412.6\hat{j} - 257.9\hat{k}$$

Find  $(x, y, z)$  so that  $\vec{r} \times \vec{F}_R = \vec{M}_I$

$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ x & y & z \\ 0 & -50 & 80 \end{vmatrix} = \hat{i}(80y + 50z) - \hat{j}80x + \hat{k}(-50x)$$
$$= 100\hat{i} - 412.6\hat{j} - 257.9\hat{k}$$

$$80y + 50z = 100 \Rightarrow \text{line } 80y = -50z + 100$$
$$\begin{pmatrix} -80x = -412.6 \\ -50x = -257.9 \end{pmatrix} \Rightarrow x = 5.16 \text{ m}$$

# Distributed pressure force



Assume  $P$  only depends on  $x$

$$dA = L dx$$

$$P(x, y) \Rightarrow \frac{N}{m^2} \text{ or Pa or psi}$$

$$F_R = \int p dA$$

$$= \int_0^w (PL) dx$$

our old  $f(x)$  or  $w(x)$