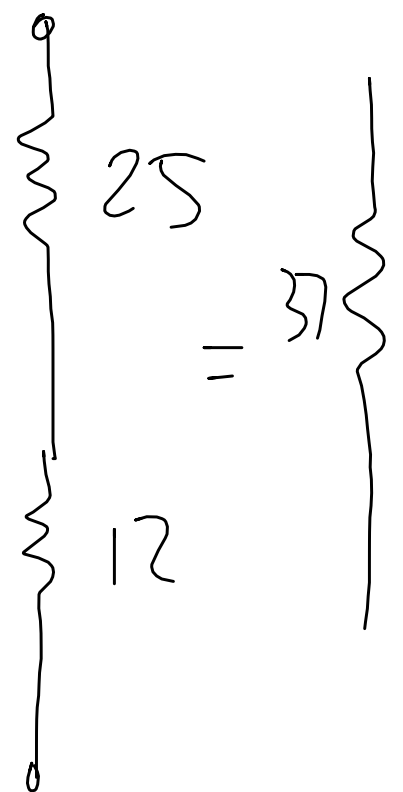
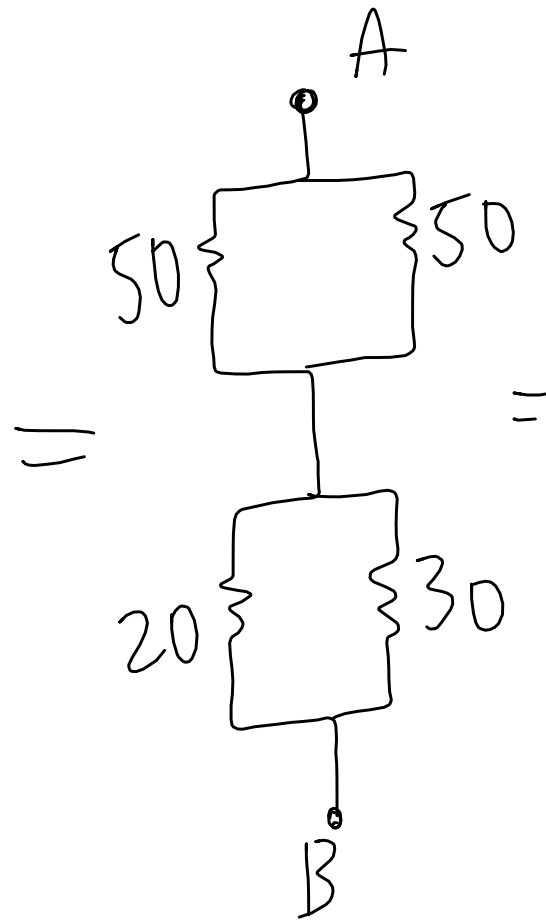
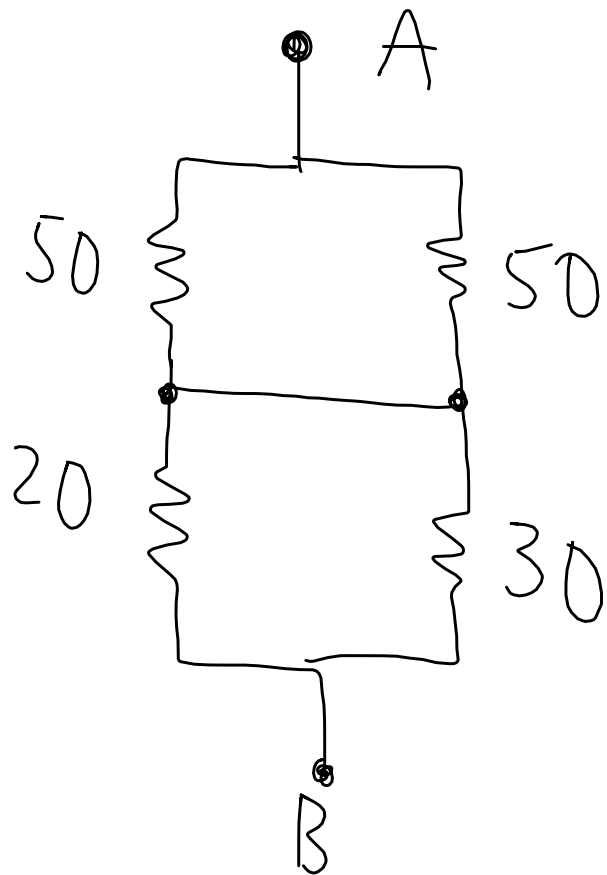


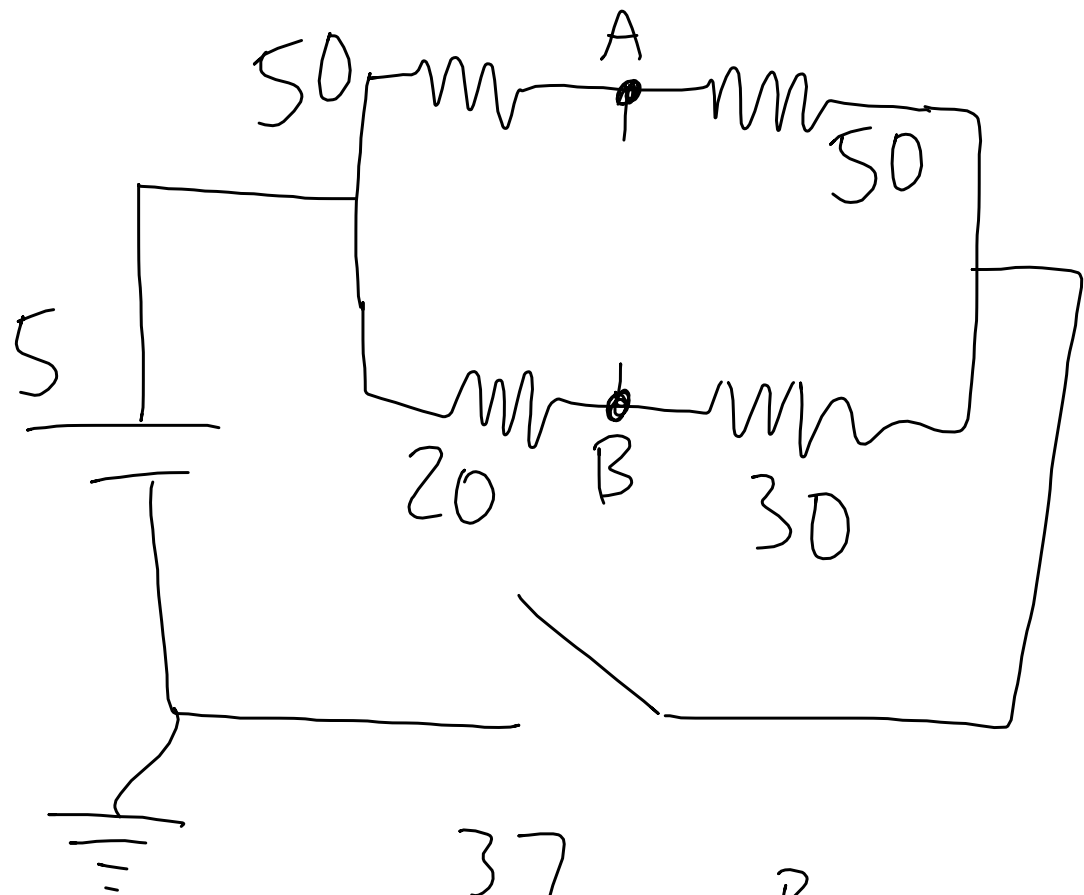
Initially uncharged

Close switch. @  $t=0$

At what  $t$  is  $V_c = 0.2V$ ?

$R_{TH} \Rightarrow$

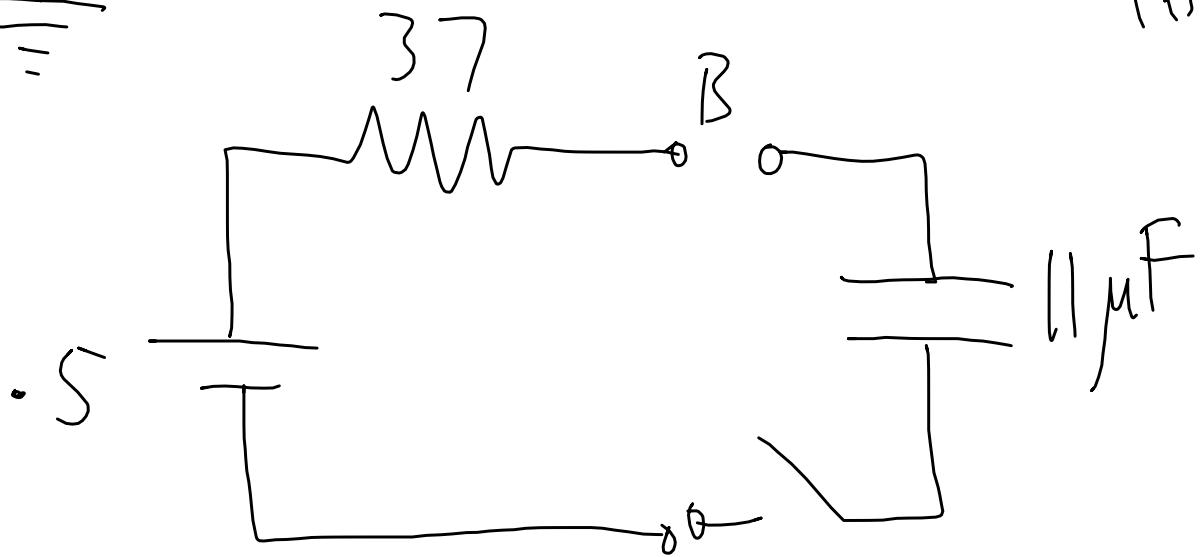




$$V_A = 2.5 \text{ V}$$

$$V_B = 3 \text{ V}$$

$$V_{TH} = .5 \text{ V} \quad (\text{B is higher})$$



$$RC = (37)(11 \times 10^{-6})$$

$$= 407 \times 10^{-6} \text{ s}$$

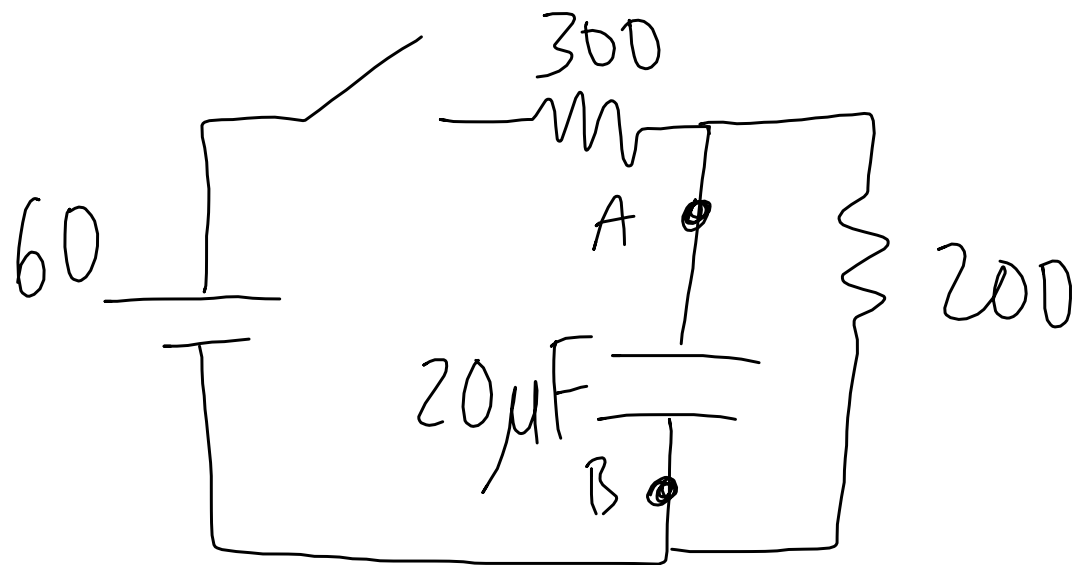
$$= .407 \text{ ms}$$

$$V_c = .5 \left( 1 - e^{-t/RC} \right) = .5 \left( 1 - e^{-t/.407 \text{ ms}} \right)$$

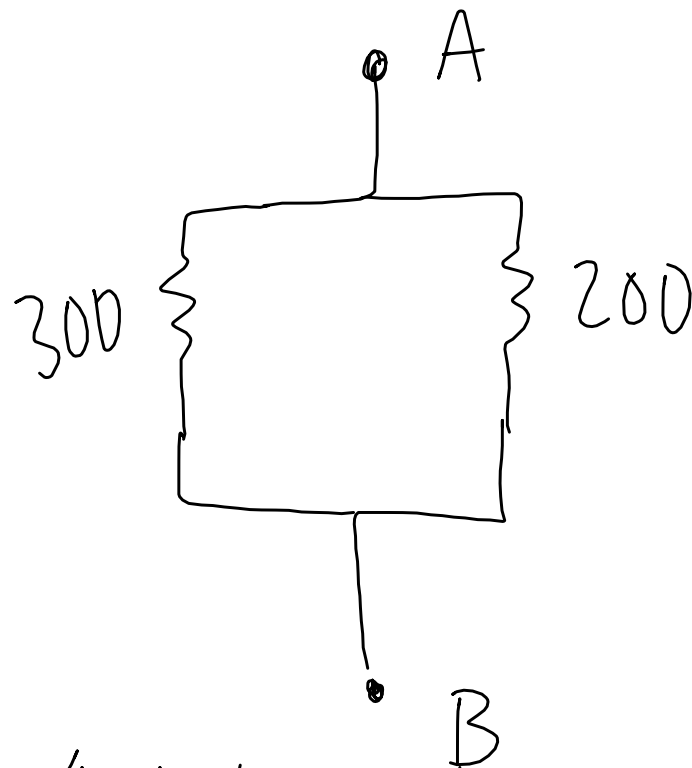
$$\text{Set } V_c = .2$$

$$.2 = .5 \left( 1 - e^{-t/.407 \text{ ms}} \right)$$

$$\frac{t}{.407} = \ln(1 - .4) \quad t = .208 \text{ ms}$$



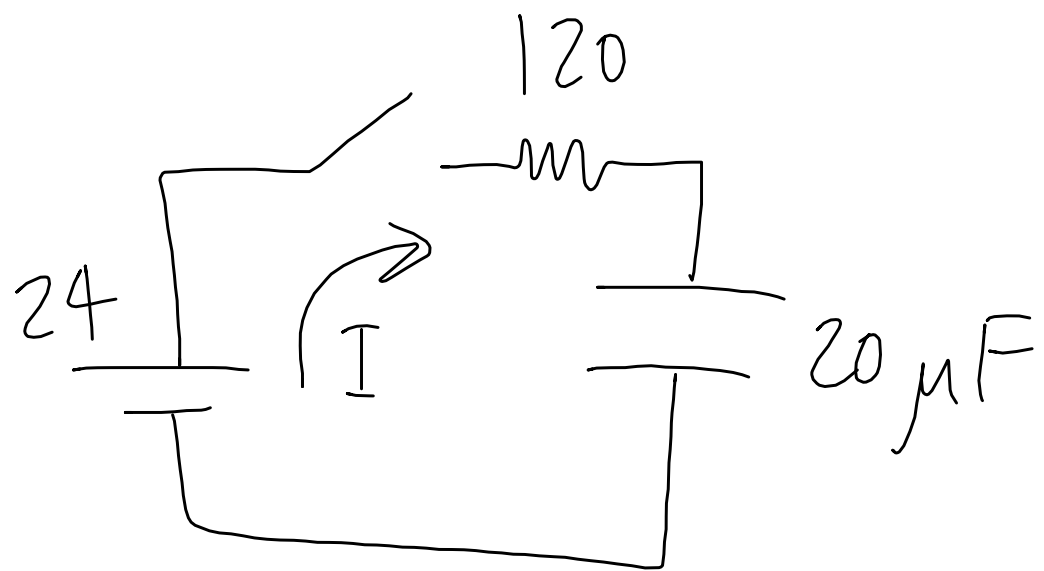
$I_{\text{batt}} @ t = 1.2 \text{ ms}$



$$\frac{200(300)}{200 + 300}$$

$$R_{\text{TH}} = 120 \Omega$$

$$V_{\text{TH}} = ? \left( \frac{200}{200 + 300} \right) 60 = 24 \text{ V}$$



$$RC = (120)(20 \times 10^{-6})$$

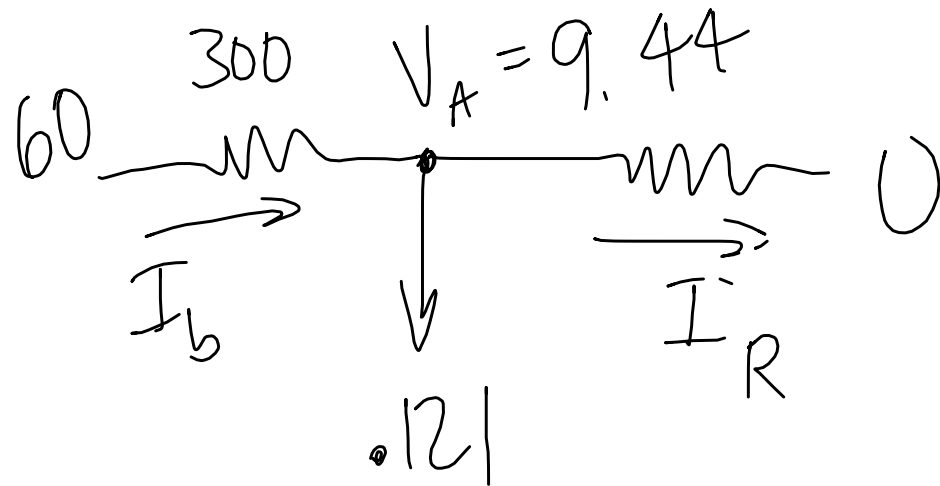
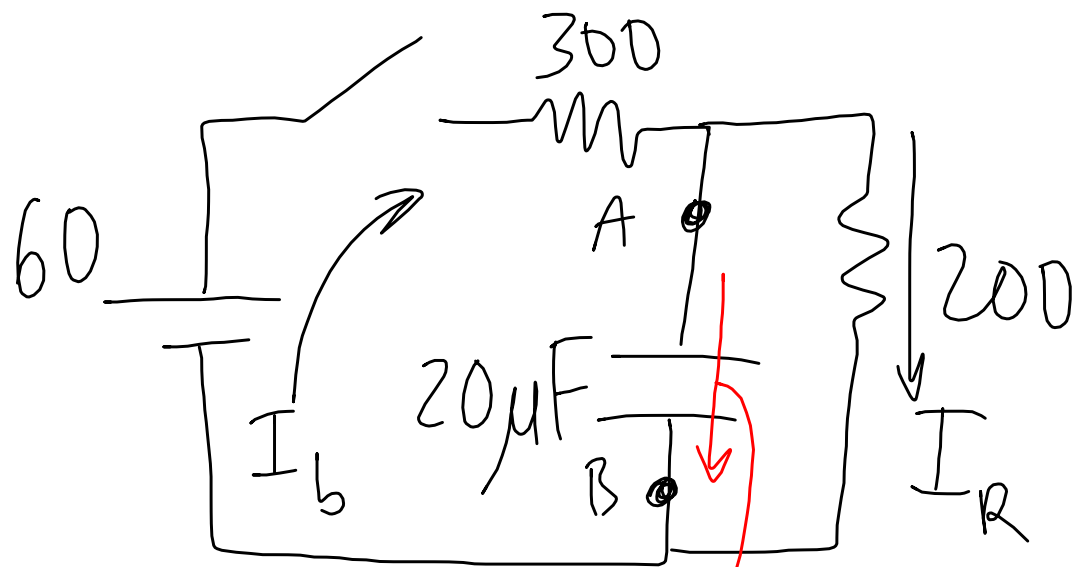
$$= 2.4 \text{ ms}$$

$$V_c = 24 \left( 1 - e^{-t/2.4 \text{ ms}} \right)$$

$$V_c(t=1.2 \text{ ms}) = 24 \left( 1 - e^{-1/2} \right) = 9.44 \text{ V}$$

$$\text{KVL: } 24 - I(120) - 9.44 = 0 \quad I = .121 \text{ A}$$

This is  $I_c$ !



$.121 A$

$$I_b = .121 + I_R$$

$$60 - 9.44 = 300 I_b$$

$$I_b = \frac{60 - 9.44}{300} = .168 A$$

Assume  $V = V_p \sin \omega t$        $\omega = 2\pi f$

$$V_{\text{Avg}} = 0$$

rms  $\Rightarrow \sqrt{V^2}$

$$\overline{V^2} = \int_0^T V_p^2 \sin^2 \omega t \, dt = V_p^2 \underbrace{\int_0^T \sin^2 \omega t \, dt}_T$$



$$\sqrt{V^2} = \frac{V_p}{\sqrt{2}}$$

Why worry about sine waves?

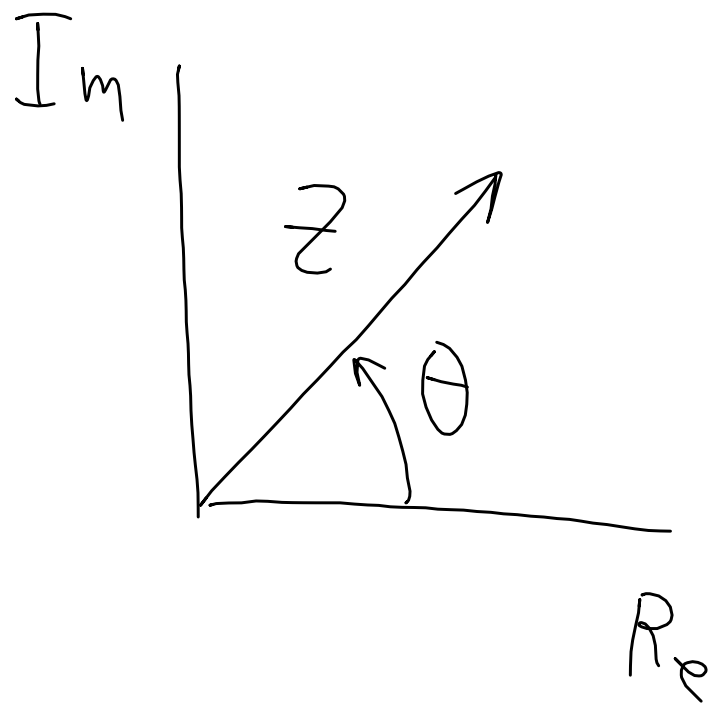
Go away from them.....

$\Rightarrow$  complex numbers

$$z = a + ib \quad i = \sqrt{-1}$$

$$z^* = a - ib$$

$$z z^* = a^2 + b^2 = |z|^2$$



$$\theta = \tan^{-1} \left( \frac{b}{a} \right)$$

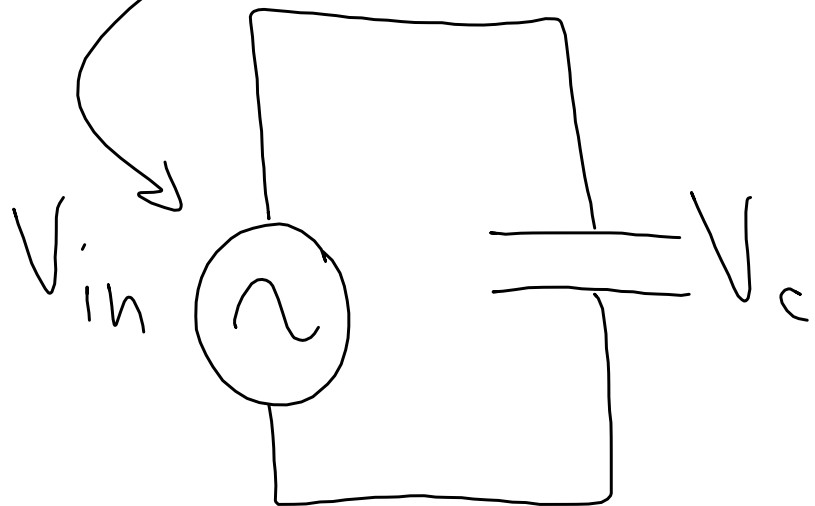
Im part

Re part

$$Z = Z_0 e^{i\theta}$$

$$e^{i\theta} = \cos\theta + i \sin\theta$$

Write  $V = V_p e^{i\omega t}$



$$V_c = V_{in}$$

$$Q = CV_c$$

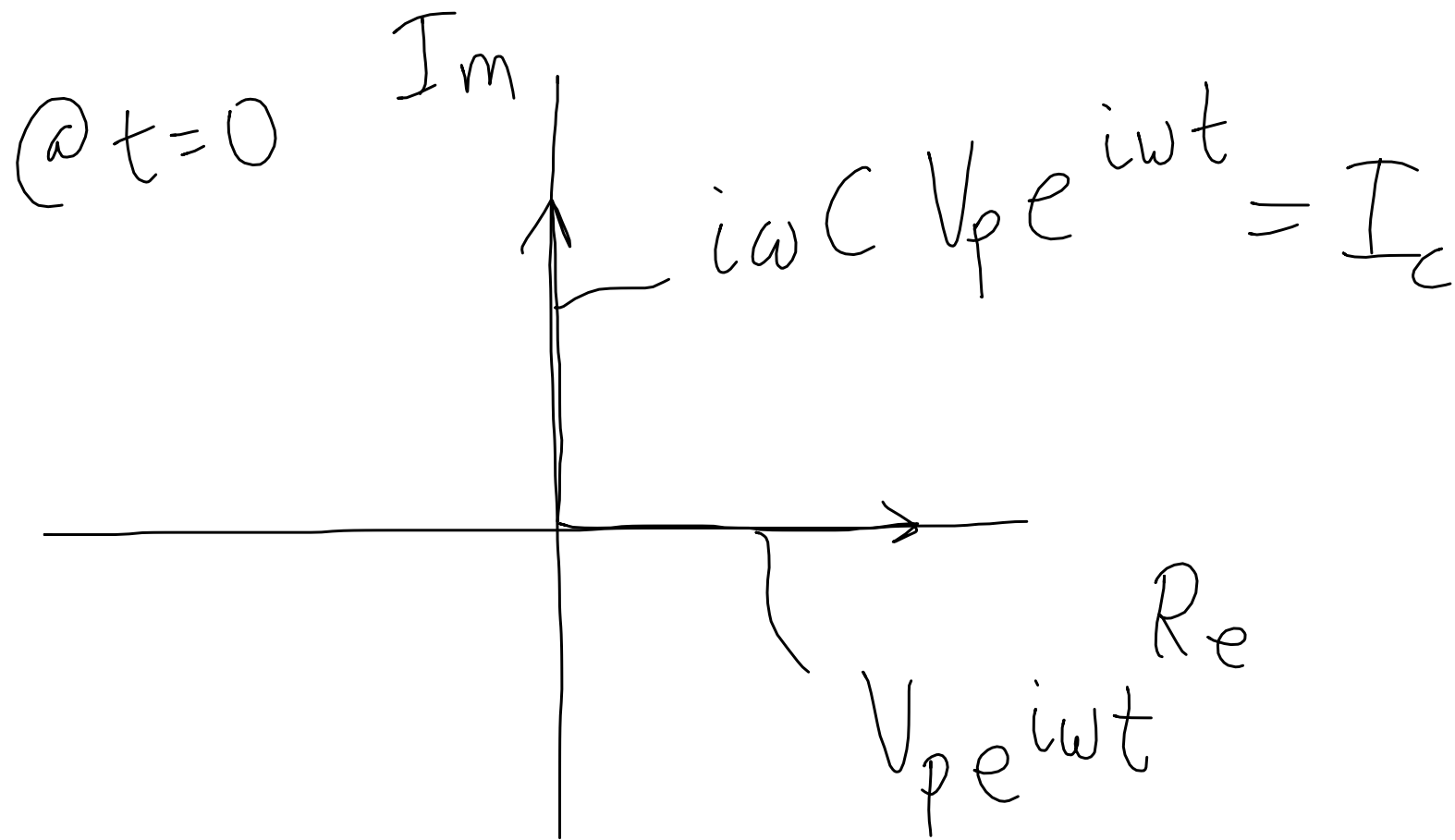
$$I_c = \frac{dQ}{dt} = C \frac{dV_c}{dt} = C \frac{dV_{in}}{dt}$$

$$I_c = C \frac{dV_{in}}{dt} = C \frac{d}{dt} (V_p e^{i\omega t})$$

$$= i\omega C V_p e^{i\omega t}$$

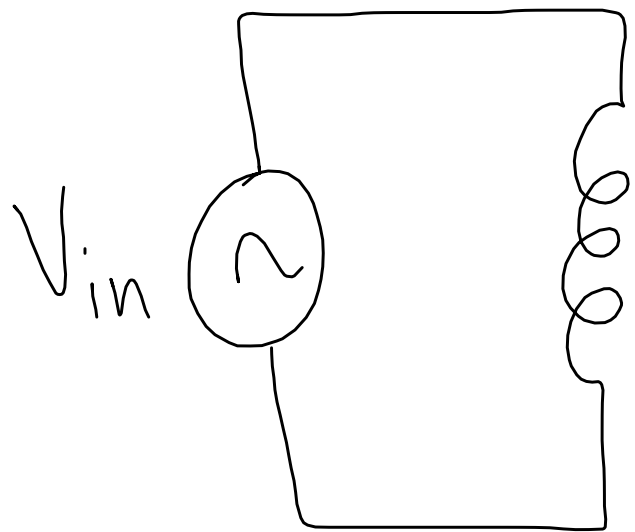
$$\frac{V_c}{I_c} = \frac{V_p e^{i\omega t}}{i\omega C V_p e^{i\omega t}} = \frac{1}{i\omega C} = \frac{-i}{\omega C}$$

$$X_c = \frac{1}{\omega C} \quad Z = \frac{-i}{\omega C} \text{ impedance}$$



Which leads,  $I_c$  or  $V_c$ ?

ELI the ICE man



$$V_L = V_{in}$$

$$V_L = L \frac{dI_L}{dt}$$

$$I_L = \int \frac{1}{L} V_L dt$$

$$= \frac{1}{L} \int V_p e^{i\omega t} dt = \frac{1}{i\omega L} V_p e^{i\omega t}$$

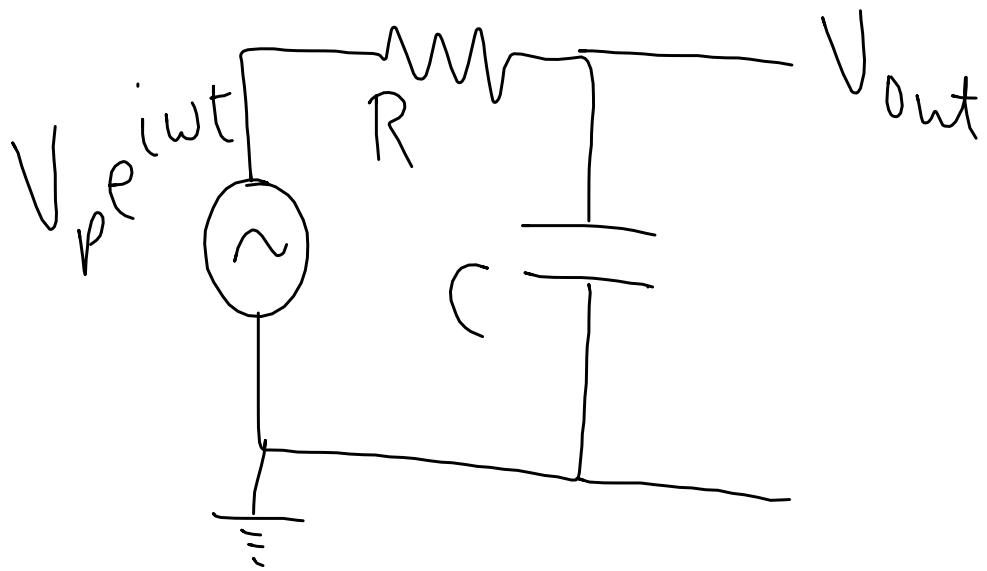
$$Z_L = \frac{V_L}{I_L} = i\omega L$$

$$X_L = \omega L \quad Z_L = i\omega L$$

Cap  $\Rightarrow Z_c = \frac{-i}{\omega C} \Rightarrow 0$  as  $\omega \rightarrow \infty$

Inductor  $\Rightarrow Z_L = i\omega L \Rightarrow \infty$  as  $\omega \rightarrow \infty$

## RC Filters



Impedances add like resistors

$Z_{total} = Z_1 + Z_2$

$\frac{1}{Z_{tot}} = \frac{1}{Z_1} + \frac{1}{Z_2}$

$$V_{out} = V_{in} \frac{Z_c}{Z_R + Z_c} = V_p e^{i\omega t} \frac{-i/\omega C}{R - i/\omega C}$$

$$\frac{V_{out}}{V_{in}} = \frac{-i/\omega C}{R - i/\omega C} = \frac{-i}{\omega RC - i} \left( \frac{\omega RC + i}{\omega RC + i} \right)$$

$$= \frac{1 - i\omega RC}{(\omega RC)^2 + 1} \left\{ \left| \frac{V_{out}}{V_{in}} \right| = \frac{\sqrt{1 + (\omega RC)^2}}{1 + (\omega RC)^2} \right.$$

$$= \frac{1}{\sqrt{1 + (\omega RC)^2}}$$